

# Analysis of diverse regulatory networks in a hierarchical context shows consistent tendencies for collaboration in the middle levels

Nitin Bhardwaj<sup>a</sup>, Koon-Kiu Yan<sup>a</sup>, and Mark B. Gerstein<sup>a,b,c,1</sup>

<sup>a</sup>Program in Computational Biology and Bioinformatics, Yale University, Bass 426, 266 Whitney Avenue, New Haven, CT 06520; and <sup>b</sup>Department of Molecular Biophysics and Biochemistry and <sup>c</sup>Department of Computer Science, Yale University, Bass 432, 266 Whitney Avenue, New Haven, CT 06520

Edited by Peter J. Bickel, University of California, Berkeley, CA, and approved February 10, 2010 (received for review September 21, 2009)

Gene regulatory networks have been shown to share some common aspects with commonplace social governance structures. Thus, we can get some intuition into their organization by arranging them into well-known hierarchical layouts. These hierarchies, in turn, can be placed between the extremes of autocracies, with well-defined levels and clear chains of command, and democracies, without such defined levels and with more co-regulatory partnerships between regulators. In general, the presence of partnerships decreases the variation in information flow amongst nodes within a level, more evenly distributing stress. Here we study various regulatory networks (transcriptional, modification, and phosphorylation) for five diverse species, *Escherichia coli* to human. We specify three levels of regulators—top, middle, and bottom—which collectively govern the non-regulator targets lying in the lowest fourth level. We define quantities for nodes, levels, and entire networks that measure their degree of collaboration and autocratic vs. democratic character. We show individual regulators have a range of partnership tendencies: Some regulate their targets in combination with other regulators in local instantiations of democratic structure, whereas others regulate mostly in isolation, in more autocratic fashion. Overall, we show that in all networks studied the middle level has the highest collaborative propensity and coregulatory partnerships occur most frequently amongst midlevel regulators, an observation that has parallels in corporate settings where middle managers must interact most to ensure organizational effectiveness. There is, however, one notable difference between networks in different species: The amount of collaborative regulation and democratic character increases markedly with overall genomic complexity.

coregulatory partnerships | hierarchy | middle managers | autocracy | democracy

In the cell, gene regulation is mediated by specialized regulators that regulate the amount or activity of their targets. For example, transcription factors (TFs) regulate the expression of target genes (TGs) by binding to their regulatory regions. Similarly, by virtue of phosphorylation, kinases regulate the activity of their targets in a posttranslational manner by adding phosphate groups to certain amino acids. These interactions can be modeled by networks with edges pointing away from regulators to their targets (1–4).

Previously, regulatory networks have been arranged into more intuitive structures like pyramidal hierarchies with the regulatory edges (chain of command) pointing downward to obtain more insight into their architecture. There have been comparisons between corporate and biological hierarchies to demonstrate strikingly similar organization (5, 6). Rearrangement into hierarchies has also been used to identify functional modules and global regulators by network decomposition approach (7). It has been shown that distinct topological units (called origons) at the root of these hierarchies are significantly affected by environmental signals (8). These origons have been shown to be responsive at various stages of adaptation of *Mycobacterium tuberculosis* allow-

ing a gradual progression of network under both replicative (growth) and nonreplicative (dormancy) states (9). Evolutionary analysis of *Escherichia coli* showed that transcriptional networks tend to grow by expansion of existing hierarchical layers, rather than addition of new layers (10). More recently, a study of TF dynamics and network architecture showed that top-level TFs in the hierarchy of yeast are relatively abundant, long-lived, and noisy whereas middle-level TFs are more well-connected and involved in higher number of GO processes (11).

In this study, we build upon the idea that depending upon the layout of regulatory edges, there are two aspects of regulation (12). In an autocracy, few top regulators influence their own set of targets directly or through a chain of influence (Fig. 1A). A social example of this kind would be a military hierarchy where general officers (such as general or lieutenant general) command over their own field grade officers (colonel, major, etc.) who in turn, are in charge of company grade officers (captain and first lieutenant). In a pure democracy, many genes exert regulatory influence on all other genes and the response is the concerted action of hundreds of genes (Fig. 1B). An example of this would be professional organizations such as a club or a scientific collaboration network without any apparent chain of command. Whereas an autocracy organizes into a neat hierarchy with well-defined levels but lacks comanagement or co-control, a democracy displays much more comanagement without well-defined levels or a clean hierarchy. It should be noted here that terms like democracy and autocracy used in this study do not exactly match the political science notions; they are defined based on analogies from Bar-Yam et al. (12).

Both autocratic and democratic scenarios are extremes and cells operate under an intermediate situation demonstrating a high degree of comanagement and coregulation with an architecture that can be organized into hierarchies (Fig. 1C). An example of this scenario would be a law firm formed by partners that have a well-defined place in the hierarchy and manage a common set of staff members such as associates and paralegals, which in turn share a team of legal assistants and interns.

In general, the presence of cross-regulation decreases the difference in information flow between nodes within a level, resulting in stress being more evenly distributed across the network. In an autocratic hierarchy (Fig. 1A), all regulatory information from the top regulators (*Squares*) to the circles pass through a specific midlevel regulator (*Triangles*). Thus, if a particular

Author contributions: N.B., K.-K.Y., and M.B.G. designed research; N.B. performed research; K.-K.Y. contributed new reagents/analytic tools; N.B. analyzed data; and N.B. and M.B.G. wrote the paper.

The authors declare no conflict of interest.

This article is a PNAS Direct Submission.

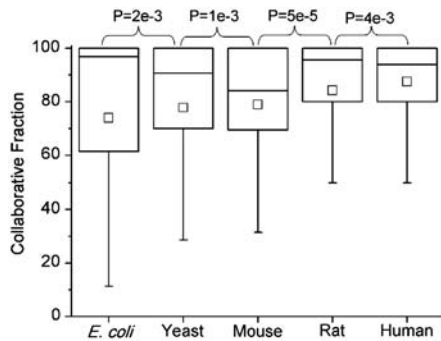
Freely available online through the PNAS open access option.

<sup>1</sup>To whom correspondence should be addressed. E-mail: mark.gerstein@yale.edu.

This article contains supporting information online at [www.pnas.org/cgi/content/full/0910867107/DCSupplemental](http://www.pnas.org/cgi/content/full/0910867107/DCSupplemental).





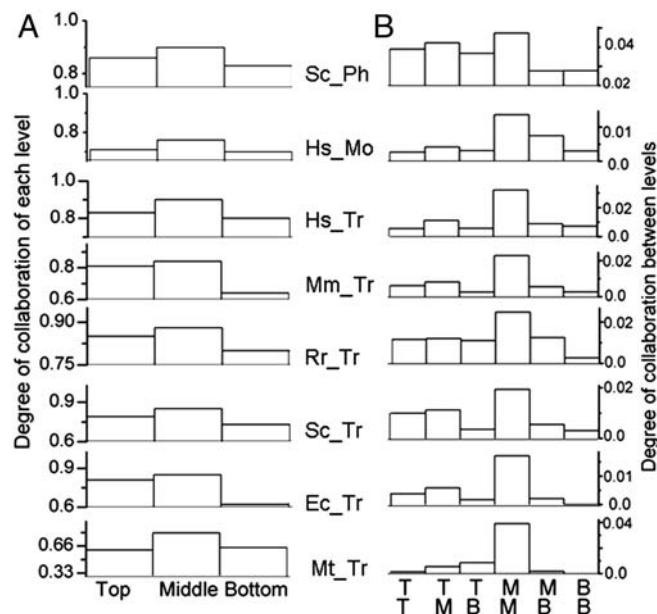


**Fig. 5.** Box-plot of the collaborative fraction (on the Y-axis) defined as the ratio of coregulated and total target genes for every regulator for all five transcriptional regulatory networks. P-values for each of the neighbors are calculated using the two sample Wilcoxon test with the null hypothesis that the distribution for species on the right (higher) is greater than that for the previous one (lower species). In other words, a low P-value indicates that the distribution for the higher species is shifted significantly toward higher values than the lower one. The smaller square corresponds to the mean of the distribution and is essentially  $D_{\text{Net-collab}}$  degree of collaboration averaged over the entire network (SI Text).

$$D_{\text{pair-collab}}^{ij} = \frac{G_i \cap G_j}{G_i \cup G_j} \text{ where } G_a \text{ is the set of targets of regulator } a.$$

Fig. S5 plots the histogram of  $D_{\text{pair-collab}}^{ij}$  and shows that a fairly good fraction of  $D_{\text{pair-collab}}^{ij}$  lies between the extremes of 0 and 1, suggesting that cellular regulatory hierarchies are intermediates between autocratic ( $D_{\text{collab}} \sim 0$ ) and democratic ones (high  $D_{\text{collab}}$ ).

**Propensity of Each Level to Be Collaborative.** We next wanted to determine which hierarchical level has the highest collaborative propensity. For this purpose, we define degree of collaboration for a level  $L$  as the average of the  $D_{\text{collab}}^i$  for all nodes  $i$  in level  $L$ ,  $D_{\text{Level-collab}}^L = \langle D_{\text{collab}}^i \rangle_i \forall i \in L$ . Not surprisingly, we found that in all five species, the middle level showed the highest propensity to be collaborative (Fig. 6A). In other words, it is the



**Fig. 6.** Collaborative tendencies of and between various levels. (A) Normalized collaborative propensity for each level,  $D_{\text{Level-collab}}^L$ . (B) Degree of collaboration between different levels,  $D_{\text{betw-level-collab}}^{L,M}$ . Network names indicated in the middle follow the same notation as in Fig. 2.

target genes of the middle level that are coregulated by other regulators the most.

**Coregulation Collaborations Within and Across Different Levels.** Next, we examined which two levels have highest coregulation tendencies between them. To investigate inter- and intralevel coregulation patterns, we defined degree of collaboration between the levels  $L$  and  $M$  as

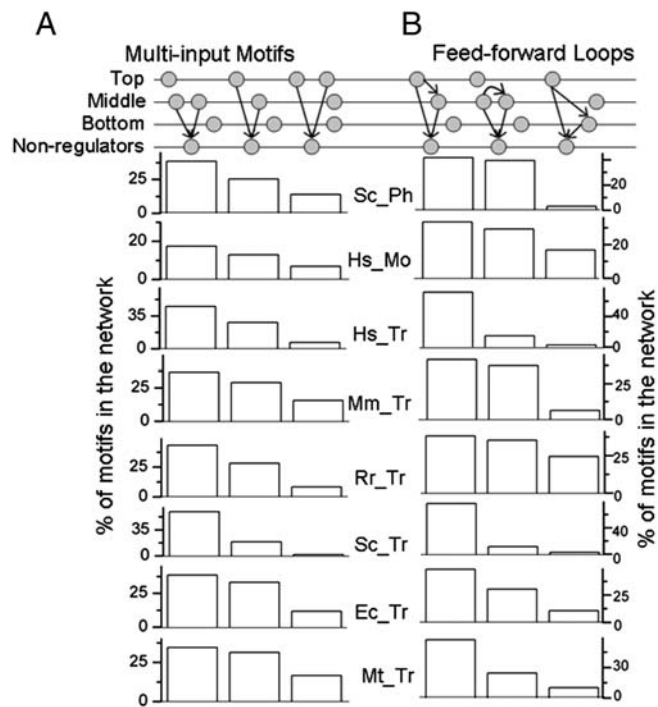
$$D_{\text{betw-level-collab}}^{L,M} = \frac{\sum_{A \in L} \sum_{B \in L} \frac{G_A \cap G_B}{G_A \cup G_B}}{|L| \cdot |M|}$$

where  $G_i$  is the number of genes regulated by regulator  $i$ , and  $|X|$  is the total number of regulators in level  $X$  (Fig. 3C).  $D_{\text{betw-level-collab}}^{L,M}$  is essentially the ratio of the number of genes coregulated by two regulators (from the same or different levels) and the union of their target genes summed over all such pairs of regulators from the two levels. Note that it is normalized for the size of each level.  $D_{\text{betw-level-collab}}^{L,M}$  varies between 0 (no coregulation collaborations between two levels) and 1 (all the targets of either level are regulated by the other level and also vice versa). A higher  $D_{\text{betw-level-collab}}^{L,M}$  between any two levels indicates a higher propensity between the regulators from those levels to coregulate their target genes.

Interesting patterns are observed for all five species and for all regulatory networks. First, we find that the highest degree of collaboration is between regulators from the middle level (Fig. 6B). In other words, it is most frequent for regulators in the middle level to pair up to regulate their common target genes. Second, the next two highest degrees of collaborations exist between middle and top level, and between regulators both from the top level. Finally, regulators that are both from the bottom level have the lowest tendency to coregulate. It is reasonable that middle-level regulators have a high degree of collaboration because of the large amount of cross talk in this level. Interactions between middle level regulators represent the “computational core” of the regulatory network. Bottom-level regulators, on the other hand, tend to activate terminal differentiation cascades, so lack of coregulation between bottom-level regulators is also reasonable. Each bottom-level regulator acts upon a different cellular process, and we expect minimal interaction between them. Similar observations are also obtained for an alternative approach of building the hierarchy (see *Robustness of Methodology and Incompleteness of Data*).

All these above findings are also readily seen in nonbiological hierarchies such as a corporate hierarchy. It has been shown that in a corporate setting, middle managers play a very important role and interact the most for organizational success (18–22). Middle managers play a critical role in linking the vision of top managers to the day-to-day realities of frontline managers (23, 24). Moreover, it is the junior managers that need least interaction with their peers; they only look after their own division and carry out the jobs assigned to them, which are mostly stand-alone (20).

As coregulation partnership between two regulators instantiates a MIM, we are essentially studying these motifs in a hierarchical context. Our results propose that certain kinds of MIMs are more commonly found in the regulatory networks of the five species than others. Fig. 7A lists the three kinds of most significantly present MIMs in the networks. In particular, in all networks, MIMs where both regulators come from the middle level are more frequent than the ones where one regulator is from the middle level and the top level each or the ones where both regulators are from the top level. We also examined the distribution of another kind of motif: the feed-forward loop (FFL) where a regulator regulates another regulator and they both regulate another common target (Fig. 7B). We find that the most common kind of FFL occurs between a top-level regulator and a middle-level



**Fig. 7.** Three kinds of most significantly present MIMs and FFLs in the decreasing order of their frequency. Values indicate the fraction of that particular kind of motif from all the occurrences of that class of motif (MIM). Network names indicated in the middle follow the same notation as Fig. 2.

regulator with a common target and the next most common FFL is found between two middle-level regulators. These frequencies of different kinds of MIM and FFL motifs are consistent with our observation above that middle-level regulators are most collaborative and with other previous studies (11).

**Robustness of Methodology and Incompleteness of Data.** One of the issues with studies dealing with the regulatory data that use different methodologies is the robustness of the results to the used definitions; it is often difficult to determine optimum values and definitions. To address this issue, we adapted different definitions and methodologies and repeated the analysis. In addition to above approach, we used another technique to construct hierarchies using both incoming and outgoing edges. First, all regulators were sorted in the increasing order of the incoming edges and decreasing order of outgoing edges. From this sorted list, we assigned top 30% to the top level, the middle 40% to the middle level, and the lowest 30% to the bottom level assigning the regulators with the most number of outgoing edges (and least number of incoming edges) to the top level and the ones with the most number of incoming edges to the bottom level. This addresses the issue of the top level diminishing in light of more data (when they have more incoming edges). We then calculated degree of collaboration between different pairs of levels and obtained similar results as above (Fig. S6) for specific types of networks (Fig. S7 and Fig. S8).

**Discussion**

In any given genome, the genes are regulated by regulators (which are fairly few in number) that control their expression (hence their amount) or their activity in the cell via combinatorial control where two or more regulators jointly regulate the target gene forming a coregulation networks. We have analyzed three kinds of coregulation networks for their hierarchical organization for five diverse species. These hierarchies had chains of commands going top down (or going horizontally in the middle level).

We have uncovered some interesting coregulatory patterns between hierarchical levels common between networks from different species, e.g., the most frequent coregulatory interactions are formed between two regulators from the middle level whereas the least frequent ones are observed between those from the bottom level. Because an instance of coregulation by two regulators essentially represents a MIM motif, we have placed it in a hierarchical context and shown that certain MIMs are more frequent than others. We have also shown that target genes of the middle level are coregulated the most, and their most frequent partners are the other middle level regulators. The observations reported above also seen readily in a typical social setting where middle managers interact the most with their peers to manage those below them (18–20, 25). Similarly, managers at the lowest level supervise their specific department without much co-control over the workers under other managers (20, 25). Our results are also shown to be robust to the adopted methodologies and parameters that can be user-subjective. Interestingly, the above findings are seen more or less consistent across all five organisms suggesting that the above properties are inherent to the regulatory and coregulatory networks of all living species. However, one of the differences between these species is the relative magnitudes of collaborative nature of regulators: Regulators in more complex species demonstrate a higher collaborative nature. We believe that these are due to the vast differences between the size and complexity of these genomes. For example, in yeast, the estimated number of regulators is 250 that regulate 6,000 targets bringing the average number of targets to approximately 25 where as for human the number is about 10 (2,000 regulators regulating 20,000 genes).

In spite of the above similarities between social and biological comanagement hierarchies, some differences between the two should also be noted. First, there are fewer comanagement interactions in corporate settings than in biological hierarchies—the reason being that corporate hierarchies are more modularized by geography or department, e.g., the middle manager of one region does not control the staff from other regions. Second, there is less direct control between levels that are two or more levels apart (e.g., top and bottom levels) in social hierarchies than in biological ones (e.g., the chief executive officer rarely gives direct orders to the janitor), although, indirect control certainly exists in social hierarchies. In biological hierarchies, such controls are more prevalent (e.g., multi-input motif with one node from the top level and one from the bottom level). Finally, whereas in cellular regulatory machinery, most regulators only either activate or inhibit their target, most social settings exhibit simultaneously positive and negative regulation: A boss may task an employee in certain instances and may also prohibit the same employee in some others. Exceptions are regulatory agencies such as the Food and Drug Administration or a police body that only inhibits. It would be interesting to incorporate this kind of dual (positive or negative) regulation in our model.

Nevertheless, our above observations are readily understandable through analogies to social settings. Such studies comparing biological networks and hierarchies to social ones aid to our intuition about the organization of the internal machinery of the cell and give insight into the nonrandom architecture of the biological networks.

**Materials and Methods**

**Dataset.** Various data sources were used for different species: the largest collection of regulatory data obtained from published microarray data for *M. tuberculosis* (9), *regulonDB* version 6.2 for *E. coli* (26), results of genetic and biochemical experiments as used in previous studies for yeast (2, 14, 15, 27–31), and Transcriptional Regulatory Element Database database for rat, mouse, and human (as of June 2008) (32). The protein modification network was obtained from the Human Protein Reference Database database (33). Phosphorylation data for yeast was obtained from two large scale experimental studies (34, 35).

**Network Transformation.** To transform the regulatory network into the coregulatory network, we placed an edge between two TFs if they regulate the same target gene and generated 1,000 control networks with the same degree distribution (in- and out-degree of each node) as the original regulatory network. As in previous studies, the aim was to keep only those coregulation edges that are more probable than random (14, 15). For every pair, the ratio of the number of target genes regulated in real network and the average number of target genes regulated in random networks was

calculated. Only edges with the ratio  $>1$  were retained to keep only those coregulatory collaborations that are more frequent than random ones.

**ACKNOWLEDGMENTS.** We thank the anonymous reviewers whose valuable suggestions helped improve the quality of the manuscript. This work was supported by the National Institutes of Health and the AL Williams Professorship funds (M.B.G.).

1. Babu MM, Luscombe NM, Aravind L, Gerstein M, Teichmann SA (2004) Structure and evolution of transcriptional regulatory networks. *Curr Opin Struct Biol* 14:283–91.
2. Lee TI, et al. (2002) Transcriptional regulatory networks in *Saccharomyces cerevisiae*. *Science* 298:799–804.
3. Guelzim N, Bottani S, Bourgine P, Kepes F (2002) Topological and causal structure of the yeast transcriptional regulatory network. *Nat Genet* 31:60–3.
4. Davidson E (2006) *The Regulatory Genome* (Academic, London).
5. Yu H, Gerstein M (2006) Genomic analysis of the hierarchical structure of regulatory networks. *Proc Natl Acad Sci USA* 103:14724–31.
6. Yu H, Xia Y, Trifonov V, Gerstein M (2006) Design principles of molecular networks revealed by global comparisons and composite motifs. *Genome Biol* 7:R55.
7. Ma HW, Buer J, Zeng AP (2004) Hierarchical structure and modules in the *Escherichia coli* transcriptional regulatory network revealed by a new top-down approach. *BMC Bioinformatics* 5:199.
8. Balazsi G, Barabasi AL, Oltvai ZN (2005) Topological units of environmental signal processing in the transcriptional regulatory network of *Escherichia coli*. *Proc Natl Acad Sci USA* 102:7841–6.
9. Balazsi G, Heath AP, Shi L, Gennaro ML (2008) The temporal response of the *Mycobacterium tuberculosis* gene regulatory network during growth arrest. *Mol Syst Biol* 4:225.
10. Cosentino Lagomarsino M, Jona P, Bassetti B, Isambert H (2007) Hierarchy and feedback in the evolution of the *Escherichia coli* transcription network. *Proc Natl Acad Sci USA* 104:5516–20.
11. Jothi R, et al. (2009) Genomic analysis reveals a tight link between transcription factor dynamics and regulatory network architecture. *Mol Syst Biol* 5:294.
12. Bar-Yam Y, Harmon D, de Bivort B (2009) Systems biology: Attractors and democratic dynamics. *Science* 323:1016–7.
13. Shen-Orr SS, Milo R, Mangan S, Alon U (2002) Network motifs in the transcriptional regulation network of *Escherichia coli*. *Nat Genet* 31:64–8.
14. Balaji S, Babu MM, Iyer LM, Luscombe NM, Aravind L (2006) Comprehensive analysis of combinatorial regulation using the transcriptional regulatory network of yeast. *J Mol Biol* 360:213–27.
15. Balaji S, Iyer LM, Aravind L, Babu MM (2006) Uncovering a hidden distributed architecture behind scale-free transcriptional regulatory networks. *J Mol Biol* 360:204–12.
16. Huang da W, Sherman BT, Lempicki RA (2009) Systematic and integrative analysis of large gene lists using DAVID bioinformatics resources. *Nat Protoc* 4:44–57.
17. Maslov S, Sneppen K (2005) Computational architecture of the yeast regulatory network. *Phys Biol* 2:594–100.
18. Floyd SW, Wooldridge B (1992) Middle management involvement in strategy and its association with strategic type. *Strateg Manage J* 13:153–167.
19. Pappas J (2001) Strategic knowledge, social structure, and middle management activities: A study of strategic renewal. PhD thesis (Isenberg School of Management, University of Massachusetts, Amherst).
20. Woodward J (1982) *Industrial Organization: Theory and Practice* (Oxford University Press, London).
21. Gioia DA, Chittipeddi K (1991) Sensemaking and sensegiving in strategic change initiation. *Strateg Manage J* 12:433–448.
22. Floyd SW, Wooldridge B (1994) Dinosaurs or dynamos? Recognizing middle management's strategic role. *Acad Manage Exec* 8:47–57.
23. Thompson T, Purdy J, Summers DB (2008) A Five Factor Framework for Coaching Middle Managers. *Organization Development Journal*.
24. Floyd SW, Wooldridge B (1997) Middle management's strategic influence and organizational performance. *J Manage Stud* 34:465–485.
25. Floyd SF, Wooldridge B (1992) Managing strategic consensus: The foundation of effective implementation. *Acad Manage Exec* 6:27–39.
26. Gama-Castro S, et al. (2008) RegulonDB (version 6.0): gene regulation model of *Escherichia coli* K-12 beyond transcription, active (experimental) annotated promoters and Textpresso navigation. *Nucleic Acids Res* 36:D120–4.
27. Harbison CT, et al. (2004) Transcriptional regulatory code of a eukaryotic genome. *Nature* 431:99–104.
28. Horak CE, et al. (2002) Complex transcriptional circuitry at the G1/S transition in *Saccharomyces cerevisiae*. *Genes Dev* 16:3017–33.
29. Luscombe NM, et al. (2004) Genomic analysis of regulatory network dynamics reveals large topological changes. *Nature* 431:308–12.
30. Svetlov VV, Cooper TG (1995) Review: Compilation and characteristics of dedicated transcription factors in *Saccharomyces cerevisiae*. *Yeast* 11:1439–84.
31. Teichmann SA, Babu MM (2004) Gene regulatory network growth by duplication. *Nat Genet* 36:492–6.
32. Jiang C, Xuan Z, Zhao F, Zhang MQ (2007) TRED: A transcriptional regulatory element database, new entries and other development. *Nucleic Acids Res* 35:D137–40.
33. Keshava Prasad TS, et al. (2009) Human Protein Reference Database—2009 update. *Nucleic Acids Res* 37:D767–72.
34. Ptacek J, et al. (2005) Global analysis of protein phosphorylation in yeast. *Nature* 438:679–84.
35. Fiedler D, et al. (2009) Functional organization of the *S. cerevisiae* phosphorylation network. *Cell* 136:952–63.