Matchmaking between hairballs – insights from cross-disciplinary network comparison

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Abstract

Biological systems are complex. In particular, the interactions between molecular components often form inscrutable hairballs. While important progress has been made, quite a bit of criticism and concerns have also been raised. Here we argue that one way of untangling these hairballs is through cross-disciplinary network comparison, comparing biological networks with those from other disciplines. On the one hand, such comparison allows the transfer of mathematical formalism between disciplines, precisely describing the abstract associations between entities. This allows us to directly apply sophisticated formalism developed elsewhere to biology (e.g. related to network growth and scaling). On the other hand, by examining in detail the mechanistic interactions in systems for which we have much day-to-day experience and then drawing analogies to more abstruse biological networks, network comparison allows us to leverage intuition from these systems to biology (e.g. applying social intuitions about management hierarchies to understand transcriptional regulatory networks).

Introduction

A signature of biology in the "omic" era is the shift of attention from a few individual components to a collection of constituents [1]. In the past structural biologists studied protein complexes consisting of a dozen of proteins, but now proteomic methods are able to probe the interactions between thousands of proteins. Similarly, geneticists who would previously manipulate a single gene for functional characterization can now employ high-throughput functional genomic techniques to study the relationships between all genes in an organism. In many cases, genome-scale information describing how components interact is captured by a network representation [2]. However, given the size and complexity of the cellular molecular networks probed by genomics and systems biology, gaining intuition or novel insights about biology from these hairballs is not always easy [3].

What approaches might help in deciphering hairballs? Throughout the history of science, many advances in biology were catalyzed by discoveries in other disciplines. For instance, the maturation of X-ray diffraction facilitated the discovery of the double helix and, later on, the characterization of structures of thousands of different proteins. Thus, one may wonder whether ideas in other areas of science could help us with the "hairball challenge". In this essay, we argue that, while the influx of ideas in the age of reductionism mostly originated from subfields of physics and chemistry, to understand biology via a systems perspective, we can further benefit from new catalysts coming from disciplines as diverse as engineering, behavioral science and sociology. These new ideas are centered on the concept of network.

Comparisons and analogies are not new to biology. For instance, to illustrate the principles of selection Dawkins came up with the idea of a meme, which is a unit carrying cultural information analogous to the gene in biology and which undergoes a similar form of selection [4]. This comparison has been further elaborated in the proto-field of phylomemetics, which concerns itself with phylogenetic analysis of non-genetic data [5]. Nevertheless, comparing a bio-molecular network with a complex network from a disparate field, say sociology, may sound like comparing apples to oranges. What kinds of comparison can truly deepen our understanding? The key lies at an appropriate level of abstraction and simplification.

Given the complexity of the cell, a certain level of simplification is necessary for useful discussion. The description of cellular systems can be seen as a spectrum (Figure 1). On one extreme, there is a complete three or four-dimensional picture of how cellular components and molecules interact in space and time. On the other extreme, there is a simple parts list that enumerates each component without specifying any relationships. However currently neither extreme leads to a full understanding and intuition for the system as a whole. It is widely appreciated that the characteristics of a cellular system cannot be explained by the properties of individual components – the whole is greater than the sum of its parts. On the other hand, a complete picture of biological systems in three or four-dimensions remains far too ambitious goal for the current state-of-the-art in data acquisition.

The network representation sits conveniently between these extremes. It captures some of the relationships between the components on the parts list in a flexible fashion, especially those where connectivity rather than exact spatial location determines the consequence. There are two thought processes in thinking about networks. The first focuses on mathematical formalisms and algorithmic aspects for practical problems. While physical associations between components can be viewed as a graph, mathematical thinking of networks goes beyond that by constructing networks via statistical association. This is exemplified by disease networks [6] in which a gene (genotype) and a disease (phenotype) are connected via the statistical association between the existence of genomic variants and the occurrence of the disease. Networks derived from co-expression relationships provide another example [7]. The second way of thinking about networks assumes the underlying network is the backbone of a complex system, and understanding the networks is a key to deciphering the organization principles behind the system. This is particularly the case for networks that capture the mechanistic interactions within systems, for instance, the cellular networks resulting from protein-protein interactions and transcriptional regulation.

Thinking of networks in a mechanistic way is a process of concretization – as opposed to the approach in abstract, association networks. Instead of moving away from the complete 4D-picture, concrete mechanistic networks aim to get closer to the picture. They are intended to describe and integrate many of the physical processes happening inside a living system-- for instance, the processing of information, the chemistry of metabolites and the assembly of molecular machines-- and therefore focus on incorporating various details of interactions. Adding further mechanistic detail onto a simple nodes-and-edges skeleton can be visualized as decorating edges with directionality, color, thickness etc. However, incorporating too much detail makes the description intractable. That is, the network formalism breaks down if we try to load spatial or temporal information as well as higher-order interactions onto the diagram. At a certain point, the actual four-dimensional picture is required.

The two network approaches essentially complement each other. On one hand, thinking in an abstract fashion allows one to transfer mathematical formalism readily between disciplines. This can be beneficial for the biological sciences, in that it allows the application of formalism developed elsewhere to find fruitful application in biology. On the other hand, thinking mechanistically focuses more on the conceptual resemblances between networks. Comparison of appropriately matched networks may provide additional intuition into the interactions between molecular components of cells by examining analogous interactions in complex systems for which we have more day-to-day experience.

Abstract approach: comparison leverages mathematical formalism

Let us first focus on abstract-association approach to biological networks. The power here of the network formalism lies in its simplicity. In the era of Big Data, the network is a very useful data structure with a wide variety of applications in both biology and other data intensive disciplines like computational social science.

A key comparison between various complex systems focuses on network topology. The earliest and probably most important observation is that many networks organize themselves into scale-free architectures in which a majority of the nodes contain very few connections (edges) while a few (also called hubs) are highly connected [8]. A surprisingly large number of networks that one comes into contact with have a scale-free architecture – e.g. the Internet, air transport routes and many social networks [9].

Another important notion is that of a small-world network, which has a short average path length between any two nodes. A scale-free network is a kind of small-world network because hubs ensure that the distance between any two nodes is small [10][11]. For example, the presence of hubs in the airport network makes it possible to travel between any two cities in the world within a short interval of time. However, not every small-world network is scale-free. An example of this is the mammalian cerebral cortex. The cortical neuronal network is subdivided into more than 100 distinct, highly modular, areas [12] that are dominated by connections internal to each area, with only ~20% of all connections being between neurons in different areas [13]. Each area is considered to have a primary feature, for example in processing sensory or cognitive signals. The cortical architecture has a high degree of clustering and a small average path-length yet exhibits an exponential degree-distribution [14].

The behavior of scale-free networks is dominated by a relatively small number of nodes and this ensures that such networks are resistant to random, accidental failures but are vulnerable to coordinated attacks at hub nodes [15]. In other words, just as the Internet functions without any major disruptions even though hundreds of routers malfunction at any given moment, different individuals belonging to the same biological species remain healthy in spite of considerable numbers of random deleterious mutations in their genomic information. However, a cell is not likely to survive if a hub protein is knocked out. For example, highly connected proteins in the yeast protein-protein interaction network are 3-fold more likely to be essential than proteins with only a small number of links [16].

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There are more elaborate approaches to determining centrality than just counting neighbors – e.g. most famously, the original PageRank algorithm, underlying the Google search approach (see BOX). Besides, one can try to define centrality via network paths using such quantities as "betweenness" (See BOX, influence & bottleneck). It has been reported that bottlenecks (nodes with high betweenness) in biological networks are more sensitive to mutations than the rest of the network, even more so than hubs for regulatory networks [17][18]. Apart from properties of individual nodes, it is important to define medium-scale structures called communities (See BOX, modularity). A quantity dubbed modularity attempts to measure this, comparing the number of intra and inter module links in a network [19].

A broad class of algorithms applied in biological and other data science maps properties or features to the nodes in a network (Figure 2) [20][21]. Apart from visualization, this mapping provides ways to organize the features. For instance, it has been reported that mapping somatic mutations to gene networks allow for stratification of cancer into subtypes [22]. Another important example is the inference of missing data using "guilt by association" -- the idea that nodes having similar associations in the network tend to be similar in properties. In a social context, if your friends in an online social network use a particular product, you are more likely to use this product and the advertisements you view online are personalized based on these recommendation systems [23]. In a biological context, it has been observed that cellular components within the same network module are more closely associated with the same set of phenotypes than components belonging to different modules [24]. As a result, one can infer the function of a gene or a non-coding element based on its neighbors. The so-called diseases comorbidity network [25][26][27] makes use of a similar idea. In such networks, a node represents a disease and two diseases are connected if they are carried by a same patient as shown in medical claims data. Diseases (phenotypes) found in the same module in the network may operate similarly on a molecular level.

Particularly informative network analyses have utilized 'seed' genes, a form of biological prior, to drive network creation. Instead of identifying hub genes based on connectivity, these hub genes are defined from the literature as being known to be causally implicated in a particular disease or phenotype. In one such example, genes implicated through copy-number variation in autism were used to cluster an expression network in healthy brain development in order to identify larger sets of putative autism-related genes as candidates for future investigation and diagnosis [28]. Such approaches are attractive as they maintain the power and flexibility of a network-based organizational scheme, but are grounded from the start in a particular biological context.

We can further exploit the structure of a network with data on underlying dynamical processes. In social science, online retailers are interested in using purchase records to study how customers influence each other [29]. The same question is extremely common in biology, under the term "reverse engineering". For example, how can we infer the developmental gene regulatory network from temporal gene expression dynamics? Ideally, one could write differential equations to fit the temporal data. However, most functional genomics experiments do not contain enough time-points. To overcome this drawback, data mining techniques such as matrix factorization are employed. For instance, given the genome-wide expression profile at different time-points, one could project the high-dimensional gene expression data to low dimensional space and write differential equations to model the dynamics of the projections [30].

In addition to the actual dynamic processes occurring on a network, one can explore evolutionary dynamics by comparing networks. In a biological context, pairs of orthologous genes (nodes) can be used to define conserved edges, called interologs and regulogs for the protein-protein interaction and regulatory networks, respectively. Furthermore, these can be used to align networks from different species [31] and to detect conserved and specific functional modules [32] across species. Based on a large collection of aligned networks between species, a mathematical formalism has been developed to measure the evolutionary rewiring rate between networks using methods analogous to those quantifying sequence evolution. In this context, it was shown that metabolic networks rewire at a slower rate compared to regulatory networks [33].

Despite an increasing number of studies applying networks in an abstract mathematical context, concerns have been raised. A major concern of network analysis comes from the criticism that statistical patterns (e.g. the scale-free degree distribution mentioned above) offer limited insights. Other examples of these patterns include the enrichment of network motifs (small recurrent subgraphs in a network). The statistical pattern suggests that the structures are potentially interesting; nevertheless, understanding the actual functions requires studying the detailed dynamics of the constituents [34]. While this is a fair comment, it is worthwhile to point out that such patterns could be used as features in various machine-learning frameworks for all sorts of biological and clinical predictions.

More fundamentally, depending on their background, different researchers may have different understanding on the meaning of "understanding" [3]. To some mathematical proof implies understanding, for others it is statistical significance, and for a third group it is molecular mechanism. For this last group, in particular, networks have often prove frustrating because their abstract patterns don't always yield easily to precise molecular description.

As an illustration, many stress that systems biology is the study of the behavior of complex biological organization and processes in terms of underlying their molecular constituents [35]. However, the mechanistic approach to networks provide a way out of this situation allowing one to leverage the more abstract network representation to try to get it some of desired mechanistic interpretation.

Mechanistic approach: comparison gives intuition into biological complexity

The previous sections discussed universal frameworks and insights gained by applying the same formalism to biological networks as well as to various social and technological ones. Such wide-ranging insights were possible only because in the abstract approach, the detailed characterization of the nodes in the network was neglected. On the other hand, if details are added to this picture, insights about a system become more specific, and in a sense, more meaningful. However, it is typically harder to apply the same formalism equivalently to two different networks, characterized in this more detailed fashion. This situation is manifest when one tried to explain the scale-free degree distribution of various networks described above.

It is well known that the scale-free network topology can be arrived by two mathematically similar but conceptually different models. The first is the celebrated preferential attachment model [8]. The scenario can be illustrated by the airline network. Every time a new airport is created, the airlines have to balance available resources and customer satisfaction, i.e., the cost of adding a new flight and customer comfort due to connectivity between the new airport and a larger number of other airports. The most efficient use of these limited resources occurs if the new airport connects to pre-existing hubs in the network as it reduces the average travel time to any airport in the entire system. The reason why the model is called preferential attachment is because the newly created nodes prefer to connect to pre-existing hubs in the network. The second is the duplication-divergence model that explains the evolution and growth of the World Wide Web. Here, a random pre-existing node and its associated edges are duplicated -- for example, to make a webpage for a new product listed on Amazon.com, one could use a template shared by an existing product [36]. After duplication, the content of two nodes and their connections diverge but a proportion of their edges are likely to be shared [37]. Such a duplication-divergence model is mathematically equivalent to the preferential attachment model since it is more likely for a hub to increase its connectivity, simply because it is easier for the hub to find a neighbor getting duplicated. However, it provides more intuition to biological network through comparison. As gene duplication is one of the major mechanisms for the evolution of protein families, scale-free behavior in the protein-protein interaction network was proposed to arise via duplication-divergence [38]. Of course, no model is perfect. Upon analyzing the structural interfaces involved in each protein-protein interaction, one observes that there are great differences in hubs that interact with many proteins by reusing the same interface versus those that simultaneously use many different interaction interfaces. The duplication-divergence model only applies to the former situation (with the duplicated protein reusing the same interface as its parent) [39]. Nevertheless,

the example shows how intuition on biological networks can be obtained through comparison to the more commonplace network, which is conceptually much easier to understand.

More intuition from social networks

The ability to gain intuition about the often-arcane world of molecular biology by comparison to commonplace systems is even more evident in comparisons involving social networks, where people have very strong intuition for how a "system" can work. Transferring understanding of organizational hierarchy to biology is a good example of this (Figure 3). Many biological networks, such as those involved in transcriptional regulation, have an intrinsic direction of information flow, forming a natural but loose hierarchy. Likewise, society has many hierarchical structures -- e.g. a militarily command chain or a corporate "org-chart" [40]. In the purest form of the military hierarchy, multiple individuals of lower rank each report to a single individual of a higher rank and there are fewer and fewer individuals on the upper levels, eventually culminating in a single individual commanding an entire army. This structure naturally leads to information flow bottlenecks as all the orders and information related to many low-rank privates must flow through a limited number of mid-level majors. In a biological hierarchy of TFs, one sees a similar pattern, with bottlenecks in the middle, and in many cases, the bottlenecks create vulnerabilities. Indeed, it has been shown in knockout experiments that many of the bottleneck nodes in biological networks are essential [17]. Structurally, hierarchies can insulate themselves somewhat from mid-level bottleneck vulnerability by allowing middle managers to co-regulate those under them. This eases information flow bottlenecks in an obvious way -- if one major gets knocked out, the privates under him can receive orders from a second major. Moreover, many commenters have pointed out that, in order to function smoothly, it is imperative for corporate hierarchies to have middle managers working together [41]. Strikingly, biological regulatory networks employ a similar strategy by having two mid-level TFs co-regulate targets below them, and this degree of co-regulation increases with overall organism complexity [42]. Thus, one can get an intuition for the reason behind a particular biological structure through analogies to a commonplace social situation.

Moreover, further comparison provides easy intuition into the biological characteristics of regulators at different levels in the hierarchy. Conventionally, one expects the CEOs of companies to gather information from all their sources and make the widest ranging and influential decisions in the company. One also stereotypically expects people at the top of conventional social hierarchies to be the most "conservative" and resistant to change. Likewise, TFs at the top of the hierarchy tend to be more connected in the protein-protein interaction network as they modulate gene expression based upon internal and external stimuli through these interactions [40][43], to be more influential in driving gene expression and to be more evolutionarily conserved [44]. Rewiring the TF network at its upper levels also tend to have a larger effect on cell proliferation and survival [45].

More intuition from technological systems

Lying at the heart of deciphering biological networks is the mapping between architecture and function. As it is often hard to define "function" in complex biological settings, comparison with simple technological or engineered components that possess basic and well-defined functions is particularly insightful [46]. For example, consider the phosphorylation and dephosphorylation reactions of a protein by a pair of kinase/phosphatases. While the mathematical description of Michaelis-Menten kinetics can be a bit complicated, the reaction essentially sets up a sigmoidal signal-response curve that is analogous the thresholding behavior of transistors in analog electronic circuits [47]. Thus, the comparison allows us to potentially map some aspects of the logical gate structure of digital electronics to the phosphorylation network. It also helped the design of synthetic biological circuits capable of logarithmic computation [48]. Similar ideas have been employed to map a transcriptional regulatory pathway to a combination of logic gates [49].

A decade ago, Uri Alon pointed out several common design principles in biological and engineering networks such as modular organization and robustness to perturbation [50]. Robustness is a preferred design objective because it makes a system tolerant to stochastic

fluctuations, from either intrinsic or external sources. Modularity, on the other hand, makes a system more evolvable. For instance in software design, modular programming that separates the functionality of a program into independent parts connected by interfaces is widely practiced [51]. The same is true for biological networks because modules can be readily reused to adapt new functions. To shed light on how biological and technological systems share the common design principles, it is important to think about how biological and technological networks change as both are adaptive. Manmade networks like roadways and electronic circuits are thought to change according to the plan of rationale designers. In contrast, biological networks are thought to change in response to random mutations and then for the successful changes to be selected. This is analogous to the work of a tinkerer, rather than an intelligent designer. Nevertheless, the distinction is not clear-cut. There are plenty of examples showing that many of man's great innovations are the result of trial and error, and all technological systems are subjected to selection such as user requirements. In a recent review, Wagner summarized nine key commonalities between biological and technological innovation, including descent with modification, extinction and replacement, and horizontal transfer [52].

In a sense, we could picture that both the engineer and tinkerer are working on an optimization problem with similar underlying design objectives, but take different views when balancing constraints. For example, in biological networks, more connected components (as measured by their degree or betweenness) tend to be under stronger constraint than less connected ones. This is evident in numerous studies that have analyzed the evolutionary rate of genes in many networks (e.g. protein interaction and transcription regulatory networks) in many organisms (e.g humans, worms, yeast, *E. coli*) using many different metrics of selection (e.g. variation within a population or dN/dS for fixed differences) [53][54][55][56]. One's intuition here is obvious: biological systems seek to decentralize functionality, minimizing average connectivity on nodes and making the system robust to a random mutation. However, this architecture requires a few hubs to connect everything up and these more connected components are particularly vulnerable. Is this finding true in general? And if not, why? Comparison can provide insight.

Consider software systems: software engineers tend to reuse certain bits of code, leading to the sharing of components between modules, arriving at highly connected components. Analysis of the evolution of a canonical software system, the Linux kernel, revealed that the rate of evolution of its functions (routines) is distributed in a bimodal fashion; the more central components in the underlying network (call graph) are updated often. These patterns seem to hold for other software systems. For instance, in package-dependency network of the statistical computing language 'R', packages that are called by many others are updated more often (Figure 4). In other words, unlike biological networks whose hubs tend to evolve slowly, hubs in the software system evolve rapidly. What's the implication? As a piece of code is highly called by many disparate processes – i.e. modules tend to overlap -- intuitively one would expect that the robustness of software would decrease. Our first intuition is that an engineer should not meddle too much with highly connected components, However, there is another factor to consider: rational designers may believe that they can modify a hub without disrupting it (i.e. the road planner thinks construction is possible in Manhattan without too much disruption) -- in contrast to a situation where random changes dominate. Moreover, the central points in a system are often those in the greatest use and hence are in the most need of the designer's attention (and maintenance). This situation is again analogous to road networks: one sees comparatively more construction on highly used bottlenecks (e.g. the George Washington Bridge) compared to out-of-the-way thoroughfares. The discrepancy between tinkerer and engineer suggests that, as an optimization process, no approach optimizes all objectives (robustness and modularity in this case) and thus tradeoffs are unavoidable in both biological and technological systems. This is essentially the conventional wisdom – there's no free lunch [57][58].

The propensity of evolution to seek decentralization is particularly evident in genes involved in metabolic pathways, in which the highly connected hub genes have more duplicated copies and are more tolerant to loss-of-function mutations [59]. However there are many highly-conserved genes that are very well connected in physical protein-protein and regulatory networks but do not

enjoy this level of redundancy. Mutations in these genes are more likely to be deleterious, resulting in a loss-of-function, and it is therefore useful to prioritize these as potential disease drivers [60].

The concept of connectivity associating with constraint is also extremely useful for therapeutics, in which a drug targeting a highly connected target can have a very efficient effect on an entire cell, albeit often with the sacrifice of low specificity. However, the measurement of connectivity/constraint depends on the cellular process. In regulatory networks and similar systems involving information transfer, this is often better conceptualized in terms of bottlenecks, while in protein-protein interactions and similar systems involved with signaling cascades it is often better to consider hubs. An example of a chemically exploitable bottleneck in the regulatory network is the bacterial ribosome, which is the target of most antibiotics that broadly inhibit protein translation leading to the rapid death of the organism [61]. A subtler, but no less useful, route to the inhibition of protein translation is through hub proteins such as mTOR and other key gates in cellular signaling cascades that are actively exploited in therapies for ailments as diverse as breast cancer [62] to depression [63].

Conclusion

Biology is a subject with a strong tradition of utilizing comparative methods. One hundred years ago, biologists compared the phenotypes of different species. Since the discovery of DNA, biologists have been comparing the sequences of different genes, and then various 'omes' across species. Perhaps, it is a time to extend this tradition even further to compare networks in biology to those in other disciplines. In fact, efforts have already been made along this direction (Figure 5). We have described how abstract approaches that focus on simple connections between entities could allow the application of mathematical formalisms across disciplines. We then showed how mechanistic details can be placed onto these simple networks and enable them to better explain a real process such as transcriptional regulation or software code development. In this case, the networks are often too detailed to allow for direct transfer of formalisms. Nevertheless, one can gain meaningful intuition about a biological system through comparing it to a more commonplace network such as a social system using a similar mechanistic description.

Seeking comparison between biological networks, social networks and technological networks may echo the long-time fantasy of finding universality in all complex systems. Indeed, the discovery of the scale-free degree distribution in many different networks initially hinted at such direction. Very soon researchers argued that a universal model never exists: there are biological networks whose degree distributions do not follow a simple power-law [64][65]; there are simply too many ways to generate a network with a broad degree distribution [66]. Indeed, it is important to clarify certain myths for the advancement of network biology as a field [67][68]. While scale-free distribution is not universal (and the lack of fundamental laws of networks in general) sounds like a bad news, we believe that one should not be disappointed or simply turn away from network biology. As suggested by some of the examples in this essay, understanding the differences between biological networks and networks from other disciplines may be as rewarding as finding the commonality. Nevertheless, discouraging the search of fundamental laws is not healthy for science. The concept of universality has a long tradition in statistical physics literature, and the perspective of characterizing the underlying mechanisms of complex systems by a few scaling or critical exponents should very much be appreciated. In fact, apart from the degree distribution, there are still many relatively open questions. For examples, as building blocks of networks, different network motifs exhibit different occurrence frequencies [69]. It is quite remarkable that under proper normalization, the transcriptional regulatory networks constructed by experiments in different cell lines as well as different species exhibit similar patterns [70][71]. Whether it is an interesting technical artifact or an insightful clue on cellular information processing is still unknown.

What's next? We envision that these cross-disciplinary network comparisons will become increasingly common as a result of data growth. One area that is especially ripe for comparison is multiplex networks, which concatenate networks to form a multiplex structure [72][73]. This

framework is commonly used in social science in which an individual may participate in multiple social circles (e.g. family, friends, and colleagues), or in an online setting: Facebook, LinkedIn and Twitter; but it has not been very well explored in biology. Nevertheless, the fundamental structure of biological data now extends beyond a single network to multiplex structures: the multiple layers could be formed by different categories of relationships (co-expression, genetic interactions, etc.), Furthermore, biological regulation occurs at multiple levels: transcriptional, post-transcriptional, and post-translational regulation in a manner in analogous to a city with electrical networks, water pipes, and cell phone lines. We are looking forward to some of the methods developed in other contexts to be applied in biology. Apart from leveraging the ideas and methods developed in multiple disciplines through comparison, we can even imagine that comparisons will ultimately lead to real connections (i.e. not analogies) between biological networks and those in other disciplines. For instance, there is an increasing amount of attention among biologists and sociologists on the connection between genomics information and sociological information such as whether phenotypes or genotypes are correlated in friendship networks [74].

Figures Caption

Figure 1.
A spectrum of cellular descriptions. From left to right. Networks help reveal and convey the relationships between components of a biological system. Different levels of information can be represented using a network. At an abstract level, a network can denote associations between various nodes. More details, such as excitatory and inhibitory regulatory relationships, can then be layered on top of this basic network. As additional information about the nodes and the relationships between them is added, the network begins to resemble the real world entity it models. For example, the addition of 3D structural information and temporal dynamics onto a network of molecular machine components leads it to more closely resemble the molecular machine itself.

Figure 2.
Intuitions guide visualizations of a complex hairball. A mechanistic network with multiple kinds of edges (protein-protein interactions, metabolic reactions, transcription regulations, etc.) forms an ultimate hairball (left). The hairball is then visualized by scaling the size of nodes by the degree of genes (right). The red nodes are essential, and the blue nodes are loss-of-function-tolerant. The network layout was generated by Vaja Liluashvili and Zeynep H Gümüş, using iCAVE [21].

Figure 3.
Comparison between the hierarchical organizations in social networks versus biological networks illustrates design principles of biological networks. The hierarchical organization in biological networks resembles the chain of command in human society, like in military context. The top panel shows a conventional autocratic military hierarchy. The structure is intrinsically vulnerable in the sense that if a bottleneck agent (star) is disrupted, information propagation breaks down. The introduction of cross-links (blue) avoids the potential problem (middle panel) because the private at the bottom can then take commands from two different superiors above. The bottom panel shows the hierarchical organization of a biological network, with the existence of cross-links between pathways. These observations reflect a democratic hierarchy as opposite to an autocratic organization.

Figure 4.
Different evolutionary patterns in biological networks versus technological networks. The left shows the protein-protein interactions network in human [75], whereas the right is the R package dependency network specifying the proper function of a package (node) depends on (edge) the installation of another. Central nodes in a PPI network are under strong selective constraints (slow rate of evolution), whereas central nodes in the R package dependency network evolve faster. In other words, network centrality and rate of evolution is negatively correlated in biological

networks (left), but positive correlated in technological networks (right). The R package dependency network consists of all the available packages (5711) via R studio at October 2014.

Figure 5.
Interdisciplinary network comparison. A lot of papers have addressed the similarity and difference between biological networks (circle) and networks in social/technological systems (squares). Here we represent all these comparison in the form of a network, where an edge associated with references represents a network comparison in a specific context (color). Moreover, these comparisons can take place in terms of abstract approaches where formalism is used equivalently in two domains (dotted lines) or mechanistic approaches where one only seeks analogy between disciplines (solid lines).

Box 1. Network centrality
· **Degree** number of neighbors of a node. The nodes with high degrees are important like a network's hubs.
· **Betweenness** number of paths passing a node. Similar in spirit to heavily used bridges, highways, or intersections in transportation networks, a few centrally connected nodes funnel most of the paths between different parts of the network. High betweenness nodes are referred to as bottlenecks and removal of these nodes could reduce the efficiency of communication between nodes [76].
· **Influence** value measuring a node's importance by taking into account the importance of its neighbors. The PageRank algorithm is a prominent example of this characteristic. Faced with a search query, Google must decide which set of results to rank higher and place on the first results page. Originally developed in social network analysis [77], PageRank utilizes an algorithm developed to rank relevant documents based on the rank of the websites that link to this document in a self-consistent manner - i.e. being linked to by higher ranking nodes has a larger impact on the document's ranking. This algorithm has been applied to food webs to prioritize species that are in danger of extinction [78] and has also been used to rank marker genes and predict clinical outcome for cancers [79]. In biology, networks play an important role in gene prioritization, an essential process for disease-gene discovery because of limited validation and characterization resources [80]. For example, network properties (e.g. hubbiness) have been used to distinguish functionally essential and loss-of-function tolerant genes [59]. One could also prioritize uncharacterized genes based on how they are connected to characterized ones. If a gene, say, is one step away from a group of genes associated with a particular disease, it is very likely that it too is associated with this disease. The influence of a node may not be restricted to its nearest neighbors; network flow algorithms are widely used to examine long-range influence [81][82]. For instance, in a social science context, researchers use cascade-structured models to capture the information propagation on blog networks, predicting a blog's popularity [83].

Box 2. Network topology
· **Modularity** value to measure strength of network division. Apart from measuring degrees and paths, one can easily observe that social networks tend to have communities within them due to the relatively larger number of interactions between people in the same neighborhood, school, or work place. People within the same social group naturally form strong ties and, in the extreme, constitute a single cohesive group (or a fully connected graph, or clique). Analogous to these closely-knit social groups, a large number of biological components can form a single functional macromolecular complex such as the ribosome. More generally, a common feature of a large number of social, technological and biological networks is that they are composed of modules such that nodes within the same module have a larger number of connections to each other compared to nodes belonging to different modules. A quantity dubbed modularity attempts to measure this, comparing the number of intra and inter module links in a network [19].
· **Missing links** connections unobservable or missing. Another type of formalism making use of properties of nodes is link prediction. High-throughput experiments can be noisy, and the resultant networks may contain spurious links; missing data is also very common. Methods for link prediction and denoising are therefore useful. This can be done solely using network

structure. For instance, in a protein-protein interaction network, defective cliques can be used to find missing interactions and determine the parts required to form a functional macromolecular complex [84]. Moving beyond network structure, whether two nodes are connected often depends on their intrinsic properties (e.g. their gene-expression level, conservation, and subcellular localization, etc.). A number of machine learning methods (e.g. collaborative filtering [85], maximum likelihood [86], and probabilistic relational models [87]) have been proposed to combine various node and edge features for link prediction [88]. One method that has not been used much in biological sciences is stochastic block models [89]. These have been popular in computational social science for link prediction [90]. They require comprehensive gold-standards for validation and may catch-on more in the biological sciences as these develop.

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