

# **A Probabilistic Model for Characterizing Regulatory Targets of Transcription Factors from ChIP-Seq and ChIP-chip Binding Profiles**

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**To be submitted to Bioinformatics very soon**

## A Probabilistic Model for Characterizing Regulatory Targets of Transcription Factors from CHIP-Seq and CHIP-chip Binding Profiles

- Suppose that we have a set of genes  $\{g\}$ , a set of Transcription Factors (TF)  $\{t\}$ , and the binding profile of each TF  $t$  on each gene  $g$ , that is,  $S_g^t$ , we want to calculate the posterior probability of TF  $t$ 's targeting gene  $g$ ,

$$\begin{aligned}
 p(t_g = 1 | S_g^t) &= \frac{p(t_g = 1, S_g^t)}{p(S_g^t)} \propto p(t_g = 1, S_g^t) \approx \sum_{i=1}^{i=n} p(t_{gi} = 1, S_{gi}^t) \\
 &= \sum_{i=1}^{i=n} p(t_{gi} = 1) p(S_{gi}^t | t_{gi} = 1) \\
 &\propto \sum_{i=1}^{i=n} w_{gi} \times f(S_{gi}^t) = \sum_{i=1}^{i=n} w_i \times f(S_{gi}^t)
 \end{aligned}$$

$w_{gi}$  is the prior prob. that TF  $t$  targets position  $i$  of gene  $g$ , and we assume that all the genes share the same position-specific prior probabilities  $w_i$ , which is estimated by Chao by the proportion of the total amount of reads or peak heights covered at position  $i$  over all genes

# **Discriminative Semi-RBMs for Modeling Interactions between Histone Modifications and TF Bindings to Predict Gene Expression**

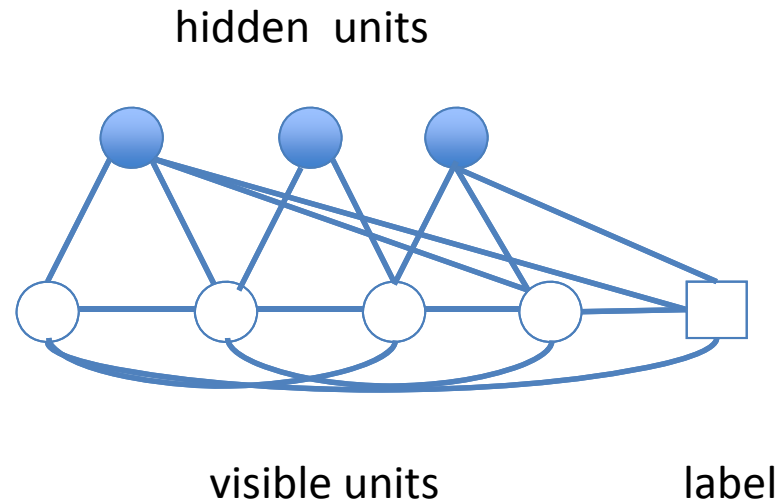
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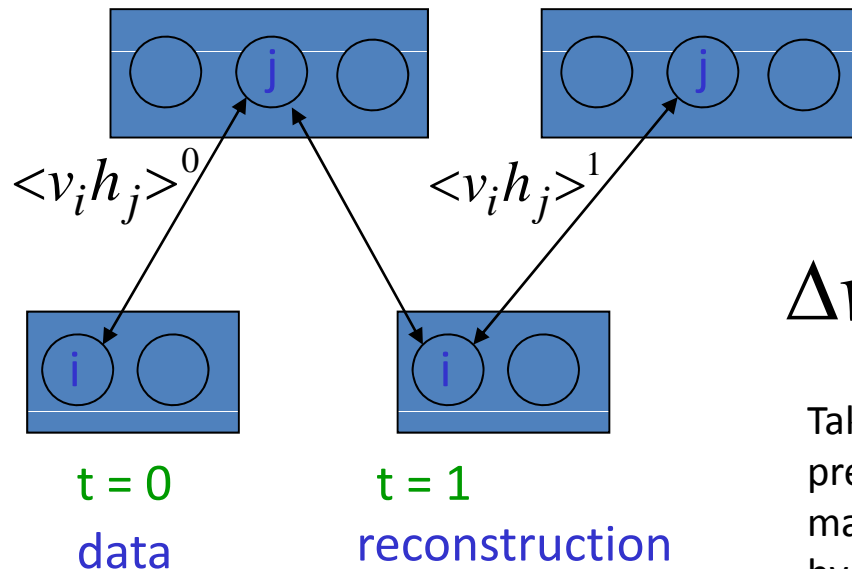
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**To be submitted to NIPS 2011 soon**

# Semi-RBMs with Lateral Connections



$$E(v, h) = - \sum_{i, j} v_i h_j W_{ij} - \sum_{y, j} l_y h_j W_{yj} - \sum_y l_y v_i v_{i'} L_{ii'} - \sum_i v_i b_i - \sum_j h_j c_j - \sum_y l_y d_y$$



$$p(v, h) \propto e^{-E(v, h)}$$

$$\Delta w_{ij} = \varepsilon (\langle v_i h_j \rangle^0 - \langle v_i h_j \rangle^1)$$

Take home message: given expression level, the model predicts that, a small number of highly interacted histone mark features are essential, and all the others are redundant by-products.